

## EFFECT OF AIR-FUEL RATIO ON TEMPERATURE DISTRIBUTION AND POLLUTANTS FOR BIOGAS MILD COMBUSTION

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### ABSTRACT

This paper examines the effect of air-fuel ratio for Moderate or Intense Low oxygen Dilution (MILD) combustion using a bluff-body burner. Exhaust gas recirculation was used to dilute the oxidizer stream prior to the combustion chamber. A low-calorie biogas fuel which consists of 60% methane and 40% carbon dioxide were used in the simulations using a Reynolds-averaged Navier–Stokes model with the realizable  $k-\epsilon$  turbulence model. The chamber temperature distribution was found to be in small ranges and almost homogeneously distributed, verifying that MILD conditions were attained. The performance was evaluated based on the level of pollutants (Unburned hydrocarbons (UHC) and carbon-mono oxide (CO)) produced and measured in the exhaust gas. Slightly lean conditions produced negligible pollutants with some excess oxygen measured in the exhaust gas. Under rich conditions, UHC and CO were produced, but when synthetic air containing oxygen with a mole fraction of 7% was used as the oxidizer instead of ordinary air, these levels were significantly reduced.

**Keywords:** MILD combustion; biogas; air-fuel ratio; exhaust gas recirculation; unburned hydrocarbon.

### INTRODUCTION

Fuel efficiency and reduced pollutants are demanded by the combustion industry due to the fuel cost and environmental regulations [1, 2]. Combustion is predicted to be the most important way of generating future energy [1, 3-6]. Fuel depletion and emission is the main issue to cater this energy need [7, 8]. Combustion technology with higher thermal efficiency and biogas fuels are possible long term solutions. A new combustion process is able to contribute to the increase of combustion thermal efficiency and reduce of the emissions. MILD combustion produces higher thermal efficiency due to re-cycling of Exhaust Gas by using exhaust gas recirculation (EGR) [7, 9-12]. Others call it flameless oxidation (FLOX) [13, 14], High-Temperature Air Combustion (HiTAC) [15, 16] and Colourless Distributed Combustion (CDC) [17, 18]. It emits low nitrogen oxides and carbon monoxide pollutant emissions [2, 19-24]. By recycle the waste heat of exhaust gases, the thermal efficiency of MILD combustion can increase by 30%, while reducing oxide of nitrogen emissions by 50% [16]. The cycle of carbon dioxide is in

close loop when emitted carbon dioxide from the combustion process will be re-used by the source of biogas when using the combustion is biogas (Low Calorific Value (LCV)) as a fuel [8, 25, 26].

In order to create a laboratory experiment's practical synthetic biogas, a mixture of 60% methane and 40% carbon dioxide was used. This ratio of synthetic biogas was also used by other researchers [27-29]. The biogas produced by feedstock normally consists of about 55% to 65% of methane, 30% to 40% carbon dioxide and 5% nitrogen. The mixture composition, measured by lambda (the Air-Fuel Ratio divided by the stoichiometric AFR) is an important parameter to indicate the combustion quality. The effect of AFR on the combustion efficiency has been studied for MILD combustion [30, 31]. The performance of combustion is very dependent on lambda, with the optimum efficiency near stoichiometric condition. High lambda will be too lean combustion and low lambda will result in unburned hydrocarbons (UHC). Due to fuel consumption, the industrial applications always use leaner combustion compared to rich combustion. The MILD combustion required lower oxygen in oxidant stream and higher temperature of the reactant mixture. Exhaust gas recirculation (EGR) has previously been used for MILD combustion [11, 15]. In this case, the combustion chamber needs to be enclosed in order to collect the exhaust gas and mixed with the supply fresh air. MILD combustion can be achieved when the oxygen level is between 3–13% [32]. The purpose of this paper is to study the combustion lambda and the pollutions for open furnace MILD combustion.

## SIMULATION SETUP

Numerical simulations are commonly used to solve many engineering problems due to cost effective, quicker and reliable solution. Many researchers have used numerical simulations to study MILD and flameless combustion [33-35]. The open chamber studied here (Figure 1) is 1.0m high and 0.6m wide and was simulated using FLUENT 14.5. The burner's data is shown in Table 1.

Table 1. Typical data for burner and combustion chamber.

Item	Data
Fuel	60% methane and 40% carbon dioxide
Oxidizers	Atmospheric and synthetic air
Fuel / air inlet	0.78 mm <sup>2</sup> / 1570 mm <sup>2</sup>
Chamber size	Diameter 600 mm, Height 1000 mm
EGR	4 EGR pipe, each with 50 mm diameter

A bluff body was used to stabilize the flame. The fuel nozzle was in the middle with a diameter of 1 mm and an annular air nozzle with an opening size of 1,570 mm<sup>2</sup>; the bluff body diameter ( $D_b$ ) was 40mm and four EGR pipes were used. In this work, the RANS equations together with the realizable  $k$ - $\epsilon$  turbulence model [36] were solved, as used previously for MILD combustion [37]. The discrete ordinate radiation model [38] and absorption coefficient of weighted sum of gray gas (WSGGM) model were used [39, 40]. The discrete ordinates radiation model solves the radiative transfer equation for a finite number of discrete solid angles in Cartesian system. The combustion was modelled using non premixed combustion with non-adiabatic flame temperature. The chemical model used is the equilibrium chemistry model couple with the probability

density function (PDF) model, as used for similar modelling in Refs. [14, 41]. In the current work, 16 species were solved at 56 grid points in mixture fraction space for a range of enthalpies to yield 24,472 potential compositions in the PDF look-up table. The temperature of the wall was set at 300K. All the governing equations were solved using the second order upwind discretization scheme for improved accuracy. The velocity-pressure coupled solver was used with the gradient least square cell based algorithm and presto pressure discretization scheme. A tetrahedral mesh with 897,703 elements was used.

The fuel supply had a 10mm diameter which tapered down to the nozzle diameter at the entrance to the combustion chamber. Air was injected through four supply pipes of 10mm diameter each at the sides of the EGR. There are two driving forces for EGR: the percentage of damper opening for the exhaust, which encourages flow to be redirected into the EGR inlets; and the fresh oxidant supply jet near the end of each EGR pipe (on the side injected into the bottom part of the EGR pipe) which induces flow through the pipes. The flue gas flow through the EGR pipe for the current results is calculated at 35.7% with the balance (controlled by a butterfly valve) allowed to flow out through the exhaust pipe on top of the burner (Figure 1). The fresh air supply then mixed with the exhaust gas (that flows downward) from the EGR pipe at the mixing area. The fuel for this burner is biogas or low calorific value gas. The biogas was produced by mixing methane and carbon dioxide. In the authors' earlier paper [31], a different LCV composition was used. In this paper, two gases are mixed: methane and carbon dioxide (Table 2). Table 2 also shows a sample composition of biogas, where there are similar levels of fuel and diluents to the syngas studied here.

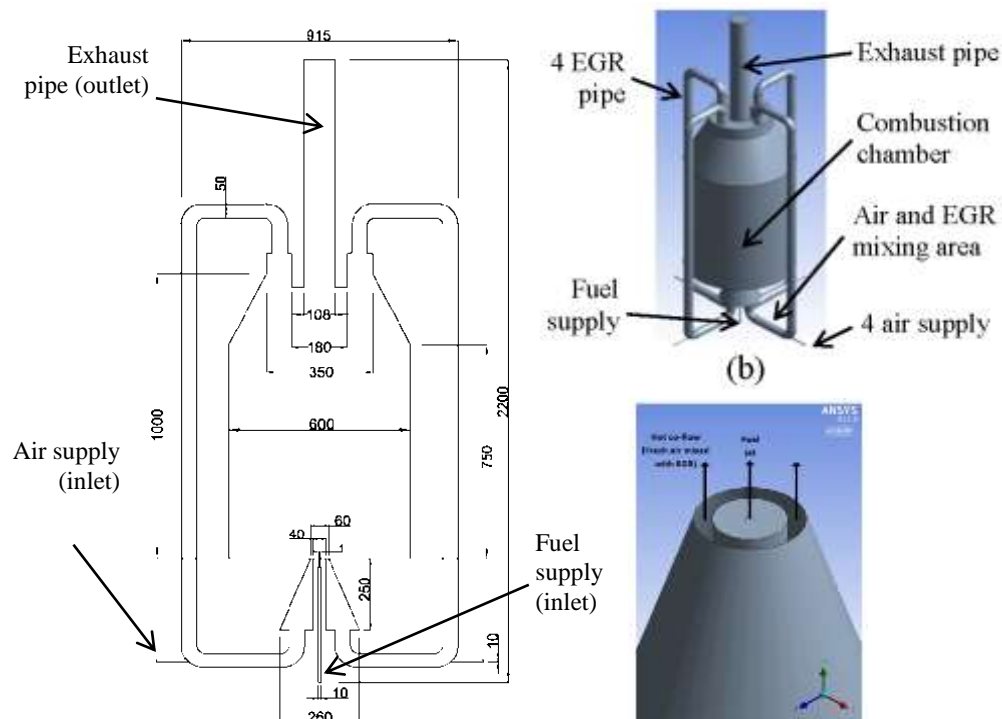


Figure 1. Burner model (a) 2D dimension in mm (b) 3D burner geometry with boundary conditions (c) air and fuel nozzle geometry and combustion flow direction.

Table 2. LCV gas composition in mole fraction .

Gas	Syngas	Biogas	LCV gas [31]
Methane ( $\text{CH}_4$ )	0.60	0.600	0.5344
Hydrogen ( $\text{H}_2$ )	0.00	0.000	0.3000
Carbon dioxide ( $\text{CO}_2$ )	0.40	0.350	0.1336
Nitrogen ( $\text{N}_2$ )	0.00	0.030	0.0130
Ethane ( $\text{C}_2\text{H}_6$ )	0.00	0.017	0.0170
Propane ( $\text{C}_3\text{H}_8$ )	0.00	0.002	0.0010
Butane ( $\text{C}_4\text{H}_{10}$ )	0.00	0.001	0.0010

The oxygen in the oxidizer stream will be diluted by EGR to the required level. In addition, synthetic air (with 3% to 15% oxygen mole fraction mixed with nitrogen) is compared with atmospheric air as the oxidizer stream. The lambda and air velocity used in this study range from 0.2 to 5.0 and 8 to 15 m/s respectively.

## RESULTS AND DISCUSSION

The results of the simulations are discussed with the main purpose to measure and analyze the lambda of the biogas combustion. A grid independence study was performed to confirm the accuracy of the mesh used in the current simulations. To conduct the parametric study, lambda was altered by varying the air and fuel supply rates. This was done for a number of different values of oxygen mole fraction in the air supply. As a preliminary study to confirm that the behaviour of the syngas is representative of a real biogas, the unburned  $\text{CH}_4$  mole fraction for high speed flow is compared in Figure 2. While the syngas slightly overestimates the values for rich conditions, the same trend to negligible amounts for stoichiometric and lean conditions is reproduced, so it can be concluded that the syngas is reasonably representative of the biogas.

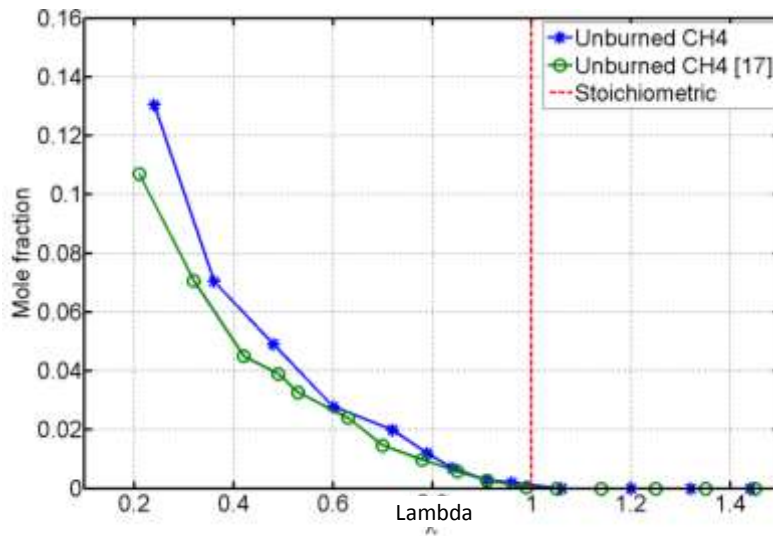


Figure 2. Unburned  $\text{CH}_4$  with atmospheric air with air inlet 20-100 m/s. Syngas, closed symbols; biogas [31], open symbols.

Figure 3 demonstrates the effects of UHC levels in the current system. In Figure 3(a), the mixing of the air supply with the EGR produces chemical reactions prior to the combustion chamber. Figure 3(b) shows a desirable operating condition with homogeneous temperature, causing the mixing of EGR and air to merely preheat the fresh supplied air. The combustion process achieves the MILD combustion state: the majority of the chamber's temperature distribution is uniformly distributed from 822K to 844K which is a variation of 2.7%. The ranges are considered to be in a uniformly small range. This is in agreement with the condition that the MILD combustion regime is achieved when the temperature distribution ranges by less than 23% (Figure 4) [16]. The highest temperature is observed slightly above the wake of the bluff-body since this is the primary mixing zone for the fuel and oxidizer. The mixture in this region is close to stoichiometric conditions, so it is inevitable that it is relatively hot. Also, this is adjacent to the recirculation region of the fuel with some of the oxidizer stream, so the increased residence time with reduced dilution causes the higher temperature. Once this mixture is further diluted with the rest of the oxidizer stream, the MILD conditions are able to dominate and reduce the temperature to the almost-constant levels detected further downstream. When there are sufficiently-high inlet velocities and sufficiently diluted oxygen, MILD conditions will develop in the chamber and the primary mixing zone is small thereby releasing only a fraction of the total heat.

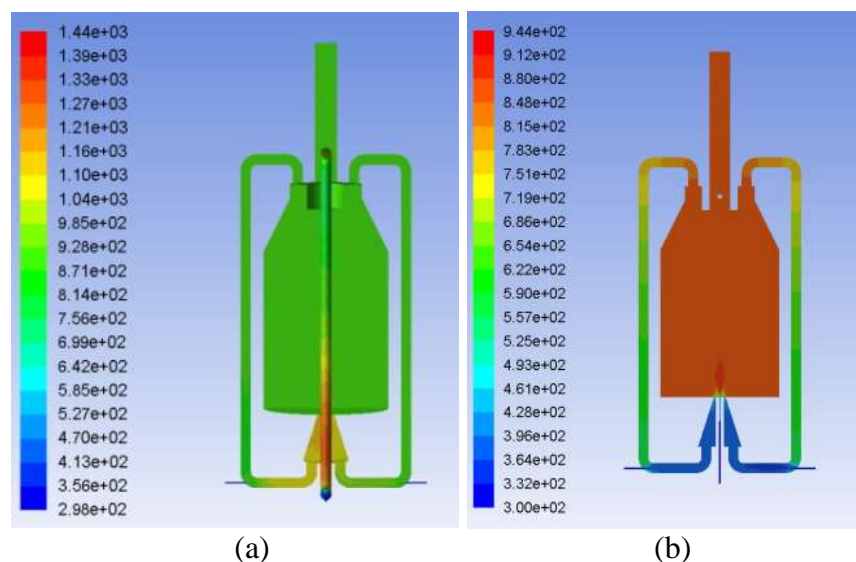


Figure 3. Temperature contours. (a) Unwanted burning between EGR and oxidizer before combustion chamber for 21% oxygen mole fraction with 10.0 m/s air inlet and lambda of 0.43. (b) Proper MILD combustion for 7% oxygen mole fraction with 10.0 m/s air inlet and lambda of 0.78.

The open furnace has been proved by the flow of streamline from air supply pipe to the exhausts opening on the top as shown in Figure 5. Figure 5(a) shows the oxidant flow smoothly from the supply inlet and exhaust opening. This was supported by Figure 5(b) that shows the velocity magnitude for the flow. The maximum and average temperatures inside the chamber and the air mixing temperature are plotted in Figure 6 for the lambda of 0.78. The average and maximum chamber temperature were almost identical at 3% inlet oxygen mole fraction with the difference increasing with inlet oxygen mole fraction. At 3% inlet oxygen, the temperature distribution and heat

produced was homogeneously uniform throughout the chamber, becoming less uniform when the oxygen mole fraction increases. The ratio of maximum-to-average temperature was less than the required 23% temperature ratio for a MILD chamber for oxygen mole fractions less than 11%. The 13% oxygen mole fraction had a temperature ratio of about 22.7% so is in the MILD regime and corresponds to the greatest increase in average temperature from the initial (air mixing) value. Beyond 13% oxygen, the efficiency decreases (lower increases in average temperature) owing to the conventional flame that is produced.

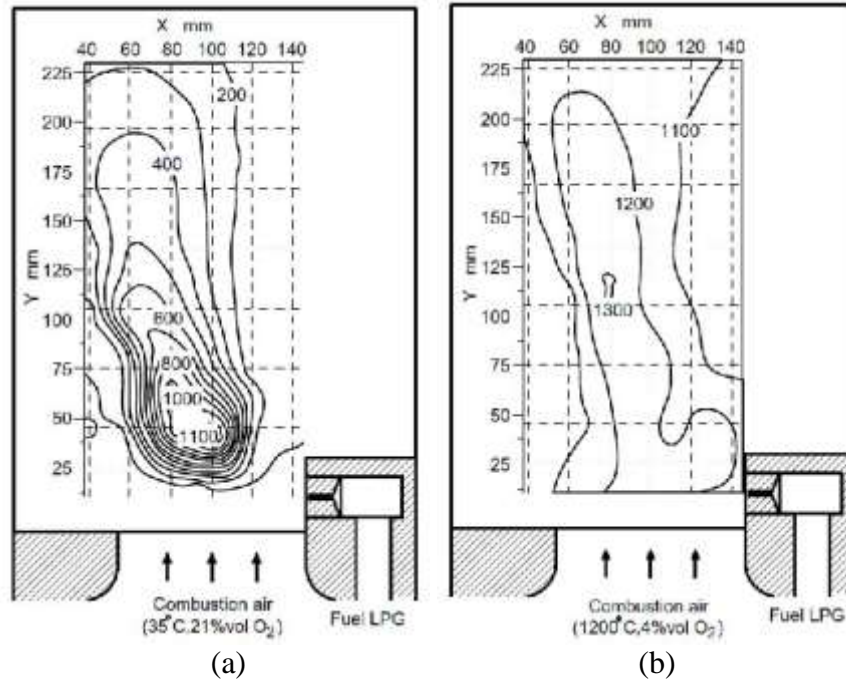


Figure 4. Combustion temperature distribution (a) conventional combustion: room temperature oxidant with 21% oxygen mole fraction (b) MILD combustion: preheat oxidant with 4% oxygen mole fraction [16].

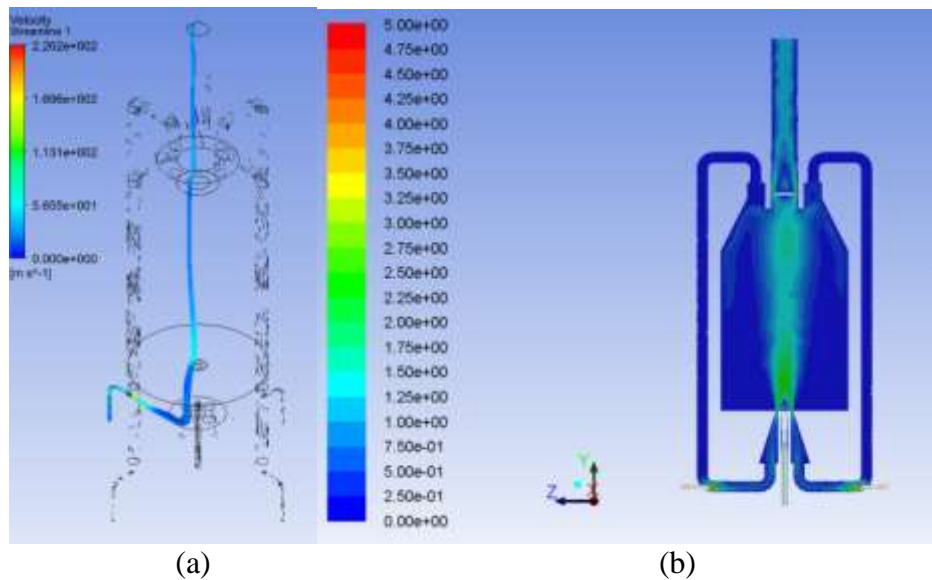


Figure 5. The flow inside the combustion chamber (a) vector plot (b) the velocity magnitude.



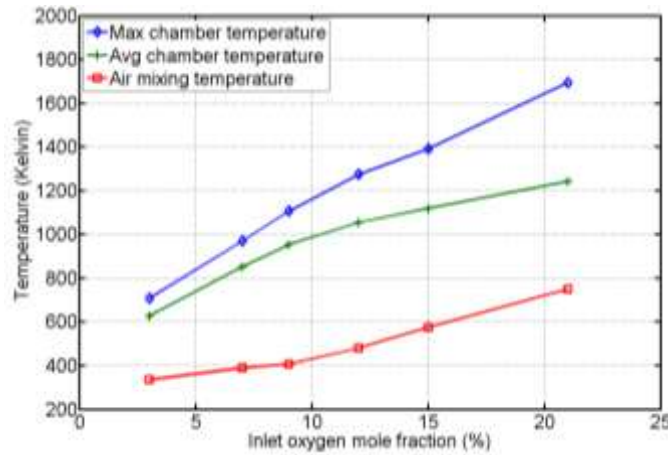


Figure 6. Maximum and average chamber and air mixing temperatures at  $\lambda = 0.78$ .

Figure 7 shows the axial location on the combustion chamber with the marking of A-A to F-F for the temperature measurement area used (and planned for the experimental work) in Figure 8. This variation in maximum and average temperatures with different inlet oxygen mole fractions is due to the lack of uniformity near the bluff body (Figure 8: note that the same scale is used). For 3% oxygen, the extra load of nitrogen keeps the temperature rise along the fuel jet to a minimum, while by 15% there is a significant variation, but this is still in MILD conditions (as noted in Table 3). For 21% oxygen, the ratio of minimum-maximum temperature was above 23% which is caused by the temperature rise almost exclusively being contained within  $r/D_b < 2$ . In this study, the wall temperature was set at room temperature, so the temperature profiles are not as uniform as for a higher wall temperature of 1300K [41], with the largest variations occurring near the bluff body (Station A-A). The effect of air supply velocity on the flame temperature was very clear. Comparing the three different air supply velocities (8 m/s, 10 m/s and 15 m/s, refer to Supplementary Material) at the same oxygen mole fraction of 3%, the higher the air supply velocity, the higher the temperature of the flame.

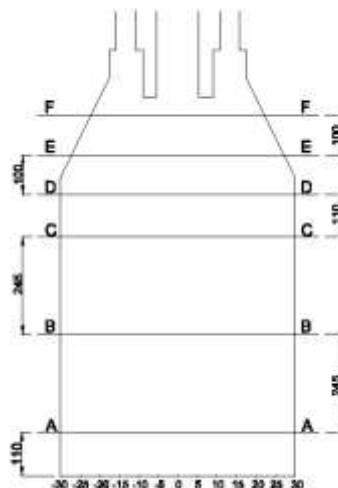


Figure 7. Chamber axial location for the temperature profile. Downstream distance from injection location,  $x/D_b$ : Station A-A = 2.8, B-B = 8.9, C-C = 15.0, D-D = 17.8, E-E = 20.3, F-F = 22.8.

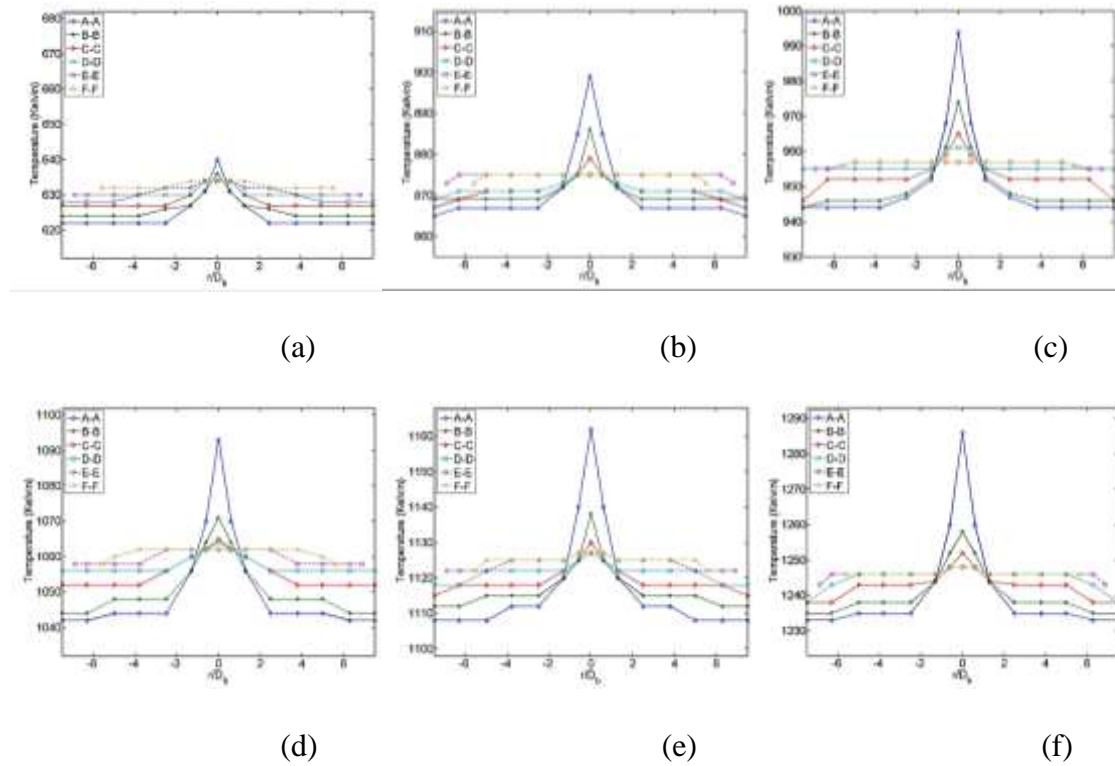


Figure 8. The temperature profile for chamber axial location of 10 m/s air supply velocity with various oxygen mole fractions in air supply stream ( $\lambda = 0.78$ ). (a) 3% oxygen (b) 7% oxygen (c) 9% oxygen (d) 12% oxygen (e) 15% oxygen (f) 21% oxygen.

Table 3. The oxygen mole fraction in air supply and MILD condition.

Conditions	Oxygen mole fraction (%)					
Oxygen mole fraction	3	7	9	12	15	21
MILD conditions	Yes	Yes	Yes	Yes	Yes	No

The temperature and combustion products are studied in Figures 9-12. Table 4 summarizes whether the MILD condition was achieved in Figures 9-12. Figure 9 shows the average chamber temperature where the air inlet has 7% and 21% oxygen mole fraction respectively. The atmospheric air produces higher temperatures, but the same trends appear: higher velocities and higher  $\lambda$  produce higher temperatures. The temperature was drastically reduced when the fuel was reduced ( $\lambda$  higher than 1.0). This is due to the combustion process was limited to lower methane supply in higher  $\lambda$  cause this lower temperature. Figures 10 and 11 show that the combustion consumes all the oxygen at lower  $\lambda$ , leaving excess oxygen as expected at higher  $\lambda$ . The excess methane and pollutant CO occurred at lower  $\lambda$  but not at higher since all methane consumes leaving excess oxygen. A small but significant amount of oxygen remains at lean conditions, consuming all the  $\text{CH}_4$ . This greater consumption of methane produces the higher temperatures.



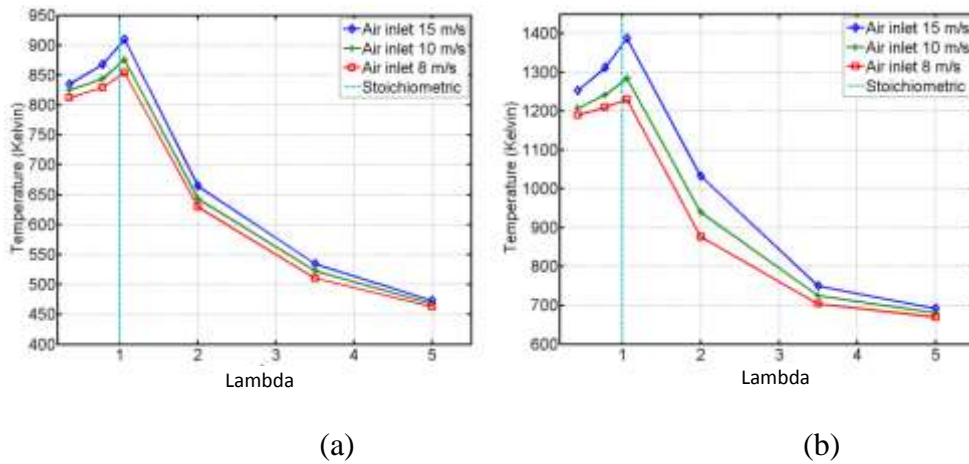


Figure 9. Chamber temperature (a) air inlet with 7% oxygen mole fraction (b) air inlet with 21% oxygen mole fraction.

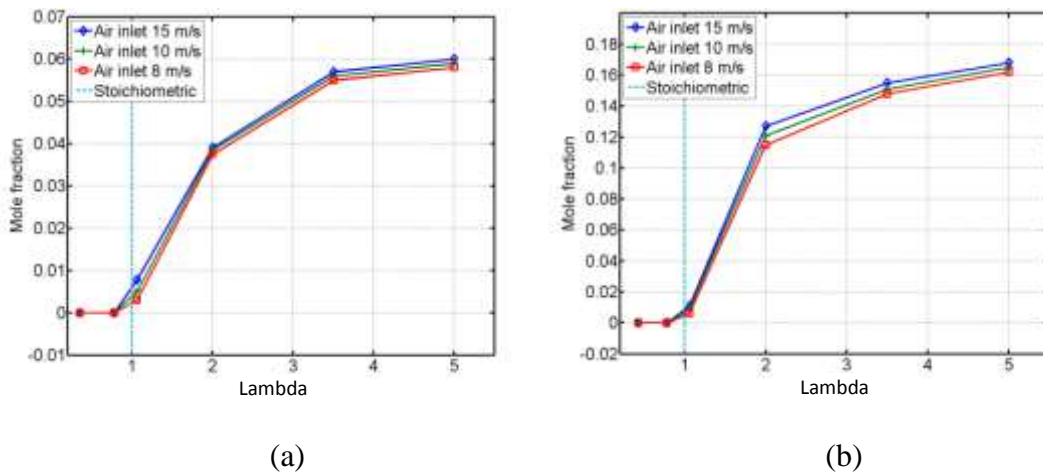


Figure 10. Excess oxygen in exhaust (a) air inlet with 7% oxygen mole fraction (b) air inlet with 21% oxygen mole fraction.

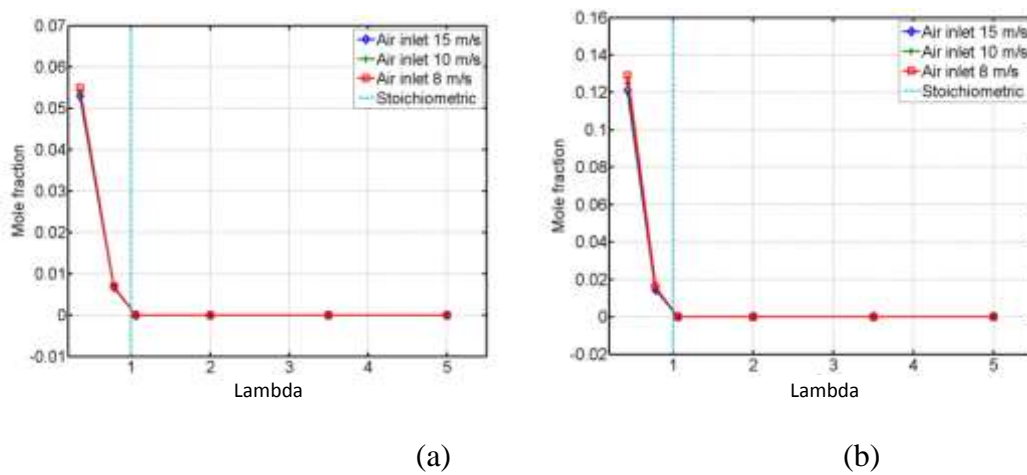


Figure 11. Unburned methane in exhaust (a) air inlet with 7% oxygen mole fraction (b) air inlet with 21% oxygen mole fraction.

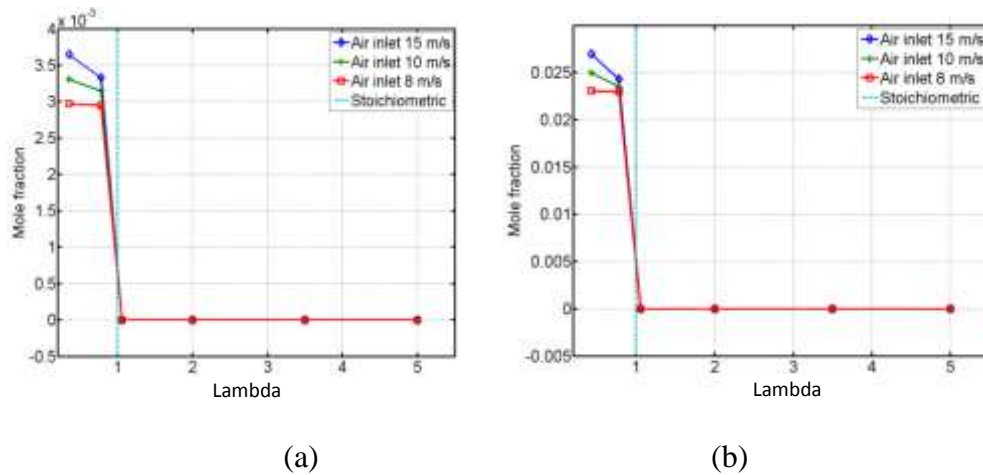


Figure 12. Pollutant carbon monoxide in exhaust (a) air inlet with 7% oxygen mole fraction (b) air inlet with 21% oxygen mole fraction.

Table 4. The oxygen mole fraction in air supply and MILD condition.

Conditions	Oxygen mole fraction	
Oxygen mole fraction	7	21
MILD condition	achieved	not achieved

Carbon monoxide is a product of incomplete combustion due to insufficient oxygen to produce carbon dioxide. The high temperature combustion for the 21% oxygen mole fraction produces more carbon monoxide [7, 13] than the 7% oxygen mole fraction (Figure 12) and CO is only produced when there is no excess oxygen (c.f. Figure 10). More results of the study were plotted for various gases which can be seen in the Supplementary Material.

## CONCLUSIONS

The flame temperature and combustion products in MILD combustion were studied numerically for varying lambda, inlet oxygen mole fraction and inlet oxygen and fuel velocity. The chemical reactions were modelled by considering chemical equilibrium based on the mixture fraction with non-adiabatic flame temperature using RANS equations and the realizable  $k-\varepsilon$  turbulence model. Under lean conditions, the pollutants CO and UHC are effectively zero, this was proved that the proposed configuration is viable for clean combustion. The present paper concludes that:

- The syngas that was used closely reproduced the behaviour of a real biogas, making this an attractive alternative for practical implementation in experiments.
- MILD conditions were found for oxygen mole fractions between 3% and 13%, which is proven by the small variations in the chamber temperature distribution. This demonstrates that an open burner can produce MILD combustion with the utilization of EGR.
- The maximum chamber temperature was near stoichiometric conditions and was reduced by approximately one-third when synthetic air (7% O<sub>2</sub>) was used instead of ordinary air, a consequence of the extra thermal load caused by the inert N<sub>2</sub>.

- iv) Under lean conditions, atmospheric air produced approximately 0.1 ppm NO, while 7%-O<sub>2</sub> air produced zero NO within numerical precision. This shows that the configuration can produce negligible pollutants without the expense of separating out N<sub>2</sub> before the combustion chamber.

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